

Proofs

Much of the *enjoyment and challenge* of geometry is found in "proving things!"

Two column proofs are the most common type of proof that we will use this year.

All two column proofs have the following elements:

- "Given" statements
- "Prove" statement
- A diagram
- Two column: Statements and Reasons
- Every statement and reason is numbered

Definitions

- need to be stated in **If - then Form**
- are *reversible*

Example: $\text{Rt } \angle = 90^\circ$

If an \angle is a $90^\circ \angle$, then it is a rt \angle .

If an \angle is a rt \angle , then it is a $90^\circ \angle$.

Index Card!!

Statements

- Always write a given for the 1st statement
- Statements need to be in a logical order
- Statements are specific
- The LAST statement is the "Prove"

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Reasons

- "Given" is always the 1st Reason
- Definitions written in "if-then" form (they are reversible!)
- Theorems (written out)

- "Addition"/ "Subtraction"
- "Assumed from diagram"
- "Same as _____"

Example Reasons

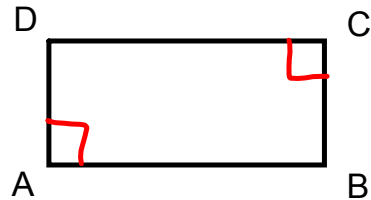
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Sample Problems

See page 25 in your textbook for Sample Problems #1 - 3

1. Given: $\angle A$ is a rt \angle
 $\angle C$ is a rt \angle

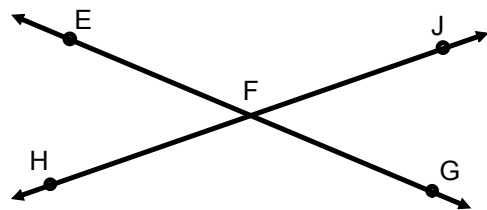
Prove: $\angle A \cong \angle C$



Statements	Reasons
1. $\angle A$ is a rt \angle 2. $\angle C$ is a rt \angle 3. $\angle A \cong \angle C$	1. Given 2. Given 3. If two angles are right angles, then they are congruent.

2. Given: *Diagram as shown*

Conclusion: $\angle EFG \cong \angle HFJ$

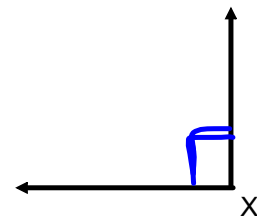
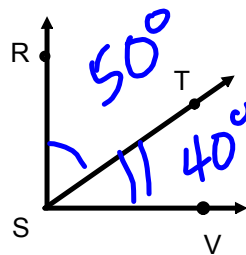


Statements

Reasons

- | | |
|--------------------------------------|--|
| 1. Diagram as shown | 1. Given |
| 2. $\angle EFG$ is a straight angle. | 2. Assumed from diagram |
| 3. $\angle HFJ$ is a straight angle. | 3. Assumed from diagram |
| 4. $\angle EFG \cong \angle HFJ$ | 4. If two angles are straight angles, then they are congruent. |

3. Given: $\angle RST = 50^\circ$
 $\angle TSV = 40^\circ$
 $\angle X$ is a rt \angle
- Prove: $\angle RSV \cong \angle X$



Statements	Reasons
1. $\angle RST = 50^\circ$	1. Given
2. $\angle TSV = 40^\circ$	2. Given
3. $\angle X$ is a rt \angle	3. Given
4. $\angle RSV = 90^\circ$	4. Addition ($50 + 40 = 90$)
5. $\angle RSV$ is a rt \angle	5. If an angle is 90 deg, then it is a rt angle
6. $\angle RSV \cong \angle X$	6. If two angles are rt angles, then they are congruent.
6. $\angle RSV \cong \angle X$	6. If two angles are rt angles, then they are congruent.

Switch to the Midpoints and Bisectors Power Point!

Exit Slip

1. List 3 "reasons" for proofs
2. What does bisect mean?
3. If two points are trisection points, what can you conclude?