

1. Grab board/marker for your group
2. Do WarmUp below

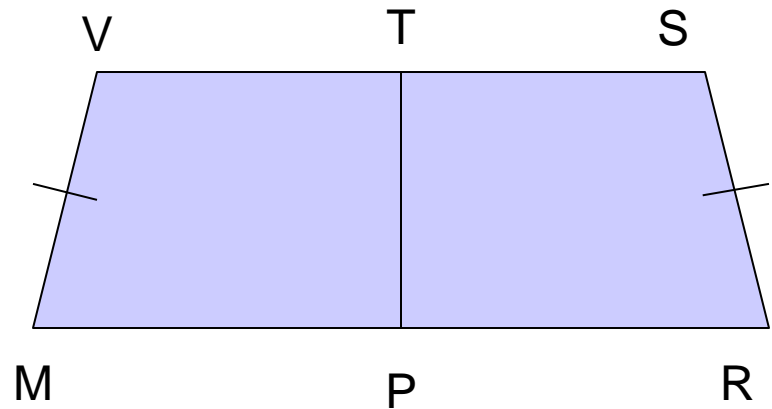
TP bisects VS and MR.

VM is congruent to SR.

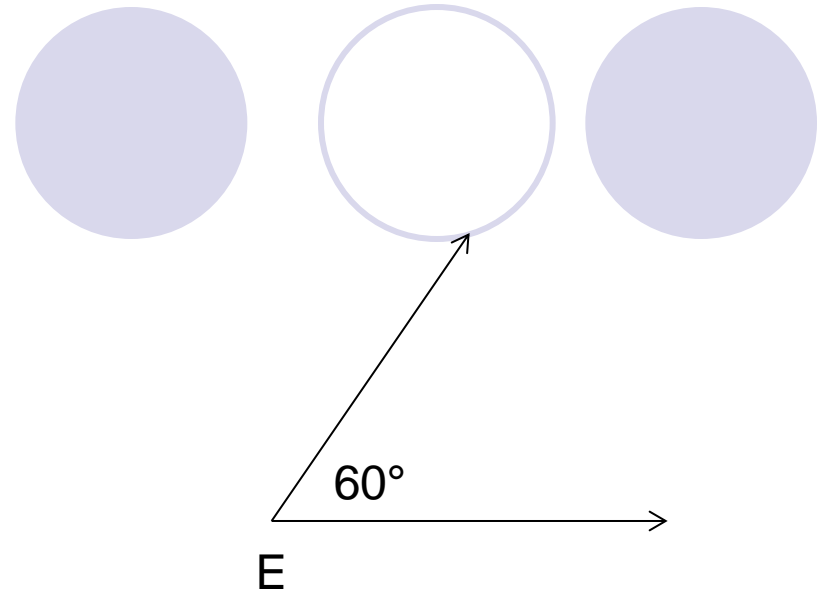
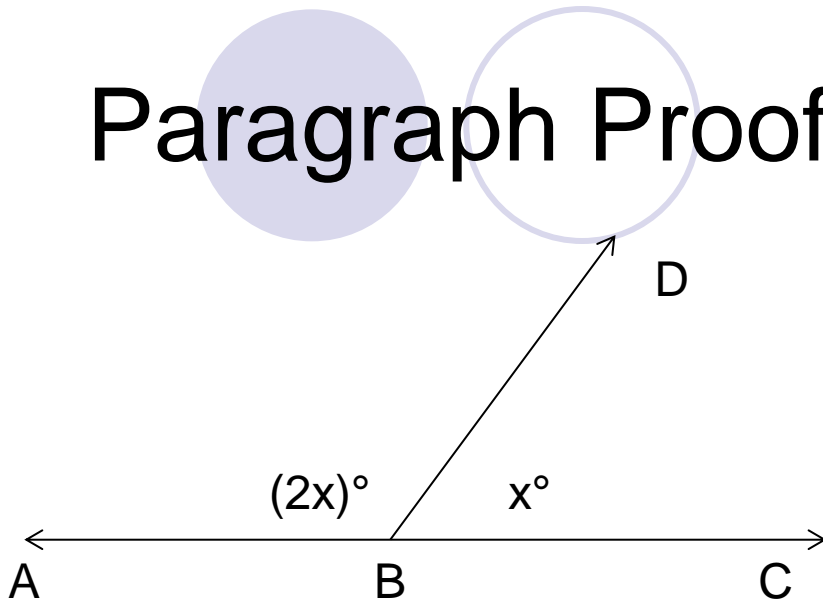
$MP = 9$, $VT = 6$

Perimeter of MRSV = 62

Find VM.



Paragraph Proof



Given: *Diagram*

Prove: Angle DBC is congruent to Angle E

According to the diagram, Angle ABC is a straight angle.

Therefore,

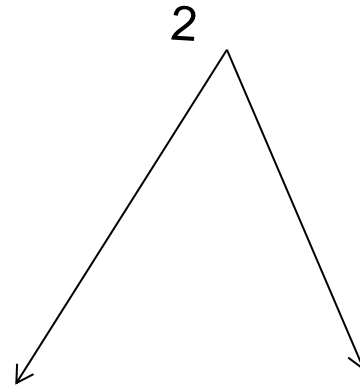
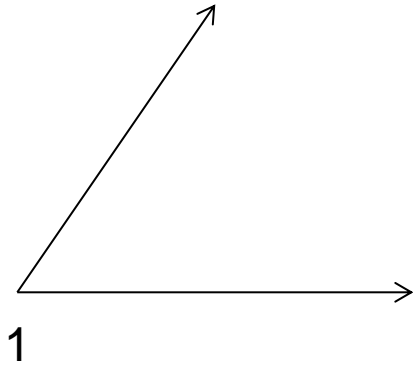
$$2x + x = 180$$

$$3x = 180$$

$$x = 60$$

Since Angle DBC = 60° and Angle E = 60° , the angles are congruent.

Paragraph Proof



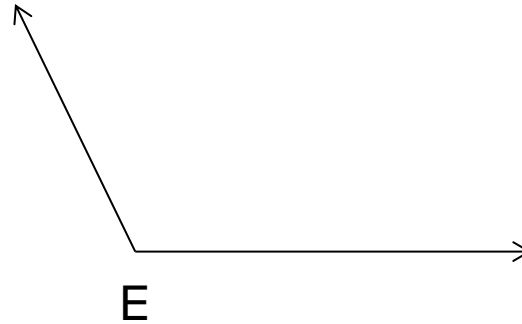
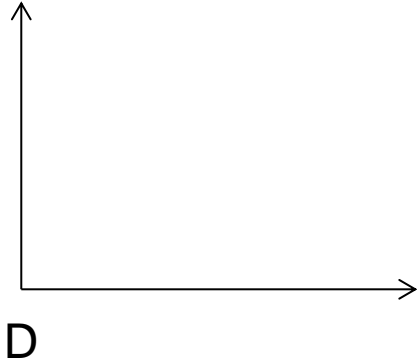
Given: Angle 1 is acute

Angle 2 is acute

Conclusion: Angle 1 is congruent to Angle 2

This conclusion cannot be proved. For example, if $m\text{Angle } 1 = 20$ and $m\text{Angle } 2 = 30$, they are both acute but Angle 1 is not congruent to Angle 2. (*Counterexample*)

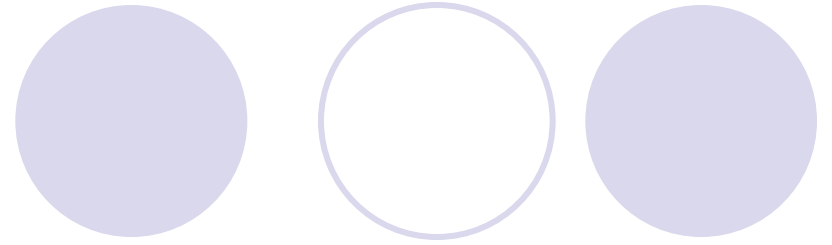
Paragraph Proof



Given: Angle D is 90°
Angle E is obtuse
Prove: Angle D is congruent to Angle E

This conclusion can be proved *false*. Since Angle E is obtuse, its measure is greater than 90. Since Angle D and Angle E have different measures, they are not congruent.

On Your Own:



- Do p.37 #2 and #3 in Boss-Secretary Format

Conditional Statements



I CAN...

- Write conditional, converse, and biconditional statements

Conditional Statements

The title is centered at the top of the slide. Behind the text are five circles of varying shades of light purple. From left to right: a solid light purple circle, a hollow light purple circle, a solid light purple circle, a hollow light purple circle, and a solid light purple circle.

- A conditional statement is written in the form ***if p, then q.***
- If a given condition is met (if p), then another condition is true or an event will happen (then q).
- The if-clause is the hypothesis; the *then-clause is the conclusion.*

Conditional Statements

Ex 1.) If you don't do your homework, then
p - Hypothesis

you will get lunch detention.
q - Conclusion

Rewrite the statements in if-then form:

Ex 2.) Every multiple of 4 is also a multiple of 2.

If a number is a multiple of 4, then it is a multiple of 2.

True or False?

True

Conditional Statements

- **Ex. 3)** $x^2 = 144, x = 12$

If $x^2 = 144$, then $x = 12$

True or False?

False – why?

Counterexample: $(-12)^2 = 144$

Logical Order



- When given several related conditional statements, you must put them in logical order. The conclusion of one statement will flow into the hypothesis of the next.

Logical Order – Put the following if-then statements in order

- A. If Cameron graduates with a degree, then he will make a lot of money.
- B. If Cameron studies hard, then his grades will be good.
- C. If Cameron makes a lot of money, then he will be able to buy a new car.
- D. If Cameron attends college, then he will graduate with a degree.
- E. If Cameron has good grades, then he will be able to attend college.

-
- Logical Order:
 - B. If Cameron **studies hard**, then his **grades** will be **good**.
 - E. If Cameron has **good grades**, then he will be able to **attend college**.
 - D. If Cameron **attends college**, then he will graduate with a degree.
 - A. If Cameron graduates with a degree, then he will make **a lot of money**.
 - C. If Cameron makes **a lot of money**, then he will be able **to buy a new car**.

Logical Order Ex. 2 – Put the statements in logical order.

- A. If a shape is a square, then it is a rhombus.
 - B. If a shape is a parallelogram , then it is a quadrilateral.
 - C. If a shape is a quadrilateral, then it is a polygon.
 - D. If a shape is a rhombus, then it is a parallelogram.
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- A. If a shape is a **square**, then it is a **rhombus**.
- D. If a shape is a **rhombus**, then it is a **parallelogram**.
- B. If a shape is a **parallelogram** , then it is a **quadrilateral**.
- C. If a shape is a **quadrilateral**, then it is a **polygon**.

Inverse - Converse - Contrapositive

What is the Inverse?

- The inverse of a conditional statement is formed by negating the hypothesis and the conclusion.
- The sentence *if p, then q* becomes
if not p, then not q.
- *State the inverse of the following conditional statements:*
- **Ex. 1)** If it is sunny today, then Julie will go running.
Inverse – If it is **not** sunny today, then Julie will **not** go running

Converse

A decorative graphic at the top of the slide consists of six circles in a row. The first, third, and fifth circles are filled with a light purple color, while the second, fourth, and sixth circles are hollow with a light purple outline. A vertical black line extends downwards from the center of the first circle.

What is the converse?

- The converse of a conditional statement is formed by switching the places of the hypothesis and conclusion.
- The sentence *if p, then q* becomes ***if q, then p.***

Converse

State the converse of the if-then statements:

- **Ex. 1)** If a polygon has five sides, then it is a pentagon.
 p - hypothesis q - conclusion

Converse – If a polygon is a pentagon, then it has five sides.
 q - conclusion p - hypothesis

True or False?

True

Converse

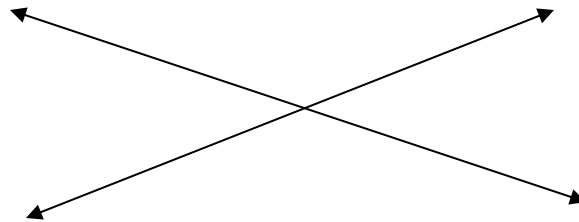
- **Ex. 2)** If two lines are perpendicular, then they intersect.

Converse – If two lines intersect, then they are perpendicular.

True or False?

False – Why?

Counterexample -



Converse



- **Ex. 3)** If a college football team wins the Big Ten Conference then they will play in a bowl game.

Converse – If a college football team plays in a bowl game then they won the Big Ten Conference.

True or False?

False – Why?

Counterexample - There are many other teams that play in bowl games!

Converse



- **Ex. 4)** If you get an A on the final exam then you will get an A in Advanced Geometry.

Converse – If you get an A in Advanced Geometry then you got an A on the final exam.

True or False?

False – Why?

Counterexample - The final exam is only 15% of your grade!

Converse

- **Ex. 5)** If three points are collinear then they lie on the same line.

Converse – If three points lie on the same line then they are collinear.

True or False?

True!

Biconditional Statements

What is a biconditional statement?

- If a conditional statement and its converse are both TRUE then they can be combined in a biconditional statement.
- The sentences *if p, then q* and *if q, then p* become

p if and only if q.

Biconditional Statements

State the biconditional:

- **Ex. 1)** If a polygon **has five sides**, then **it is a pentagon**.

Converse – If a polygon **is a pentagon**, then it **has five sides**.

Biconditional – A polygon **has five sides** *if and only if* it **is a pentagon**



Biconditional Statements

- **Ex. 2)** If three points are collinear then they lie on the same line.

Converse – If three points lie on the same line then they are collinear.

Biconditional – Three points are collinear if and only if they lie on the same line

Homework



- p. 37 #4 – 7, 9
- p. 42 #1 – 5, 8 – 12, 14