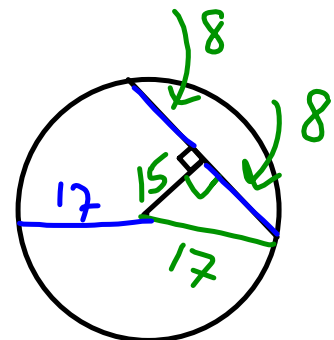


Warm Up

1. Draw Circle O
2. Draw radius OR
3. Draw diameter DM
4. Draw chord PQ (that does not go through O)
5. Find the length of a chord that is 15 cm from the center of a circle with a radius of 17 cm.



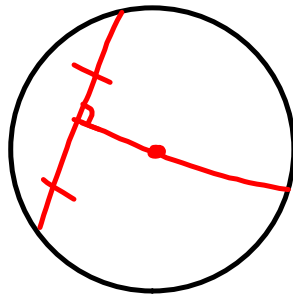
16cm

Theorems

If a radius is perpendicular to a chord, then it ● bisects the chord.

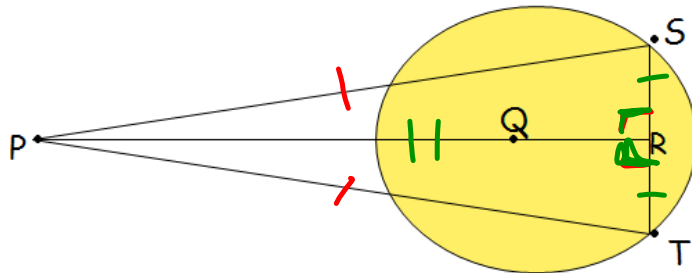
If a radius bisects a chord, then it is ● perpendicular to the chord.

The perpendicular bisector of a chord passes through the ● center of the circle.



Given: Circle Q
 $\overline{PR} \perp \overline{ST}$

Prove: $\overline{PS} \cong \overline{PT}$



Statements	Reasons
① Circle Q	① Given
② $\overline{PR} \perp \overline{ST}$	② Given
③ $\angle QPT \cong \angle QPS$	③ \perp lines form $\cong 90^\circ$ \angle 's.
④ $\overline{SR} \cong \overline{TR}$	④ If a radius is \perp to a chord then it bisects the chord
⑤ $\overline{PR} \cong \overline{PR}$	⑤ Reflexive property
⑥ $\triangle PSR \cong \triangle PTR$	⑥ SAS
⑦ $\overline{PS} \cong \overline{PT}$	⑦ CPCTC

① Circle Q

① Given

② $\overline{PR} \perp \overline{ST}$

② Given

③ $\angle QPT \cong \angle QPS$

③ \perp lines form $\cong 90^\circ$ \angle 's.

④ $\overline{SR} \cong \overline{TR}$

④ If a radius is \perp to a chord then it bisects the chord

⑤ $\overline{PR} \cong \overline{PR}$

⑤ Reflexive property

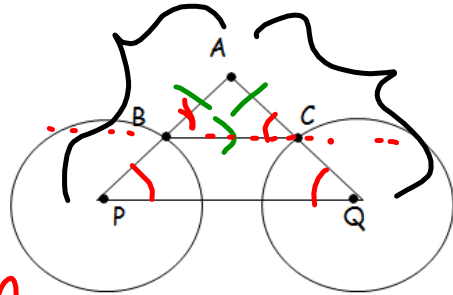
⑥ $\triangle PSR \cong \triangle PTR$

⑥ SAS

⑦ $\overline{PS} \cong \overline{PT}$

⑦ CPCTC

Given: $\triangle ABC$ is isosceles ($\overline{AB} \cong \overline{AC}$)
 (S) $\cdot P$ and Q (all radii \cong)
 $\overline{BC} \parallel \overline{PQ}$



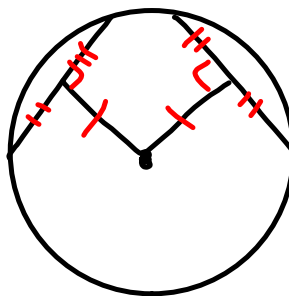
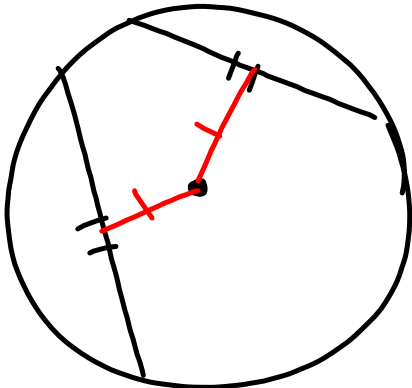
Prove: $\odot P \cong \odot Q$ ← Radii are \cong .

- | S | R |
|---|-----------------------------|
| ① $\overline{AB} \cong \overline{AC}$ | ① Given |
| ② P + Q are (S) | ② Given |
| ③ $\overline{BC} \parallel \overline{PQ}$ | ③ Given |
| ④ $\angle ABC \cong \angle ACB$ | ④ If Δ then Δ |
| ⑤ $\angle B \cong \angle P$ | ⑤ Corresponding \angle 's |
| ⑥ $\angle C \cong \angle Q$ | ⑥ Same as 5 |
| ⑦ $\overline{AP} \cong \overline{AQ}$ | ⑦ Δ then Δ |
| ⑧ $\overline{BP} \cong \overline{CQ}$ | ⑧ Subtraction Prop. |

Theorems

If two chords are equidistant from the center, they are congruent.

If two chords of a circle are congruent, then they are equidistant from the center.



Given: $\odot O, \overline{AB} \cong \overline{CD}$

$$OP = 12x - 5, OQ = 4x + 19$$

Find: $OP = 12(3) - 5 = \boxed{31}$

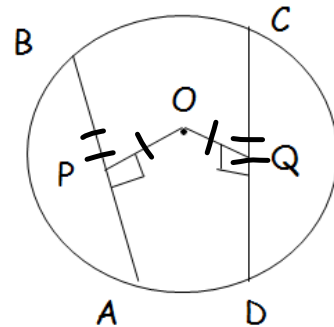
$$12x - \cancel{5} = 4x + \cancel{19} + 5$$

$$\frac{12x}{4} = \frac{4x}{4} + \frac{24}{4}$$

$$3x = x + 6$$

$$\begin{array}{r} -x \\ \hline 2x = 6 \end{array}$$

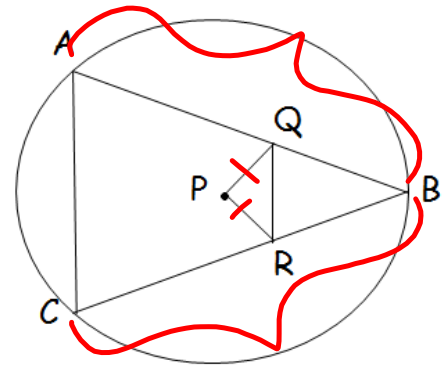
$$\boxed{x = 3}$$



Given: $\triangle ABC$ is isosceles with base \overline{AC} .

$\odot P, \overline{PQ} \perp \overline{AB}, \overline{PR} \perp \overline{CB}$

Prove: $\triangle PQR$ is isosceles.



S	R
① $\triangle ABC$ is isos.	① G
② $\odot P, \overline{PQ} \perp \overline{AB}, \overline{PR} \perp \overline{CB}$	②
③ $\overline{AB} \cong \overline{AC}$	③ Def. of Isosc.
④ $\overline{QP} \cong \overline{PR}$	④ If 2 chords are \cong , they are equidistant from the center
⑤ $\triangle PQR$ is isosc.	⑤ Isosc. \triangle has 2 \cong sides

Homework

- pg. 443 #1, 3, ~~5, 8~~, 11, 12
P P E E P M
 5, 6, 7, 8

- pg. 447 #2-5, 11, 12
2, 3, 4, 5 M H
M P P P

- Proofs

- Easy

- Medium

- Hard

