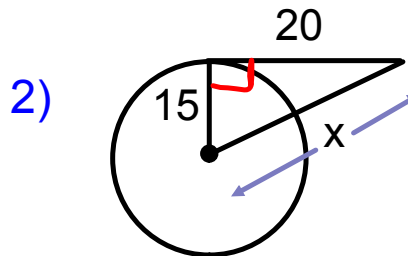
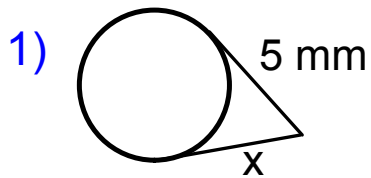


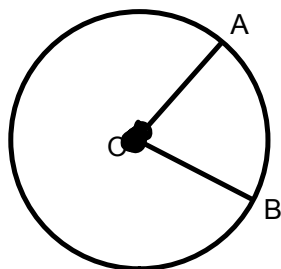
Starter

Find the value of x .



- 3) Draw two circles that are externally tangent.
- 4) Draw two circles that are internally tangent.

10-5 Angles Related to a Circle

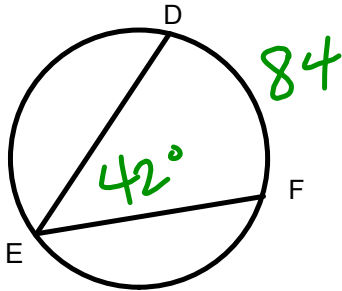


Central Angle
 $m \angle AOB = m \text{ Arc } AB$

Example:

Given $m \angle AOB = 72^\circ$, Find $m \text{ Arc } AB$



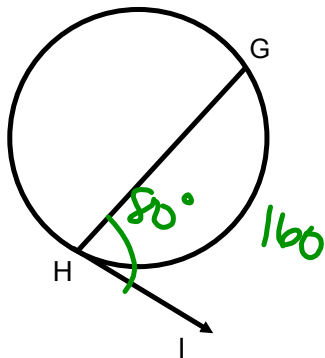


Inscribed Angle

$$m \angle DEF = \frac{1}{2} (m \text{ Arc } DF)$$

Example:

Given $m \text{ Arc } DF = 84^\circ$, Find $m \angle DEF$

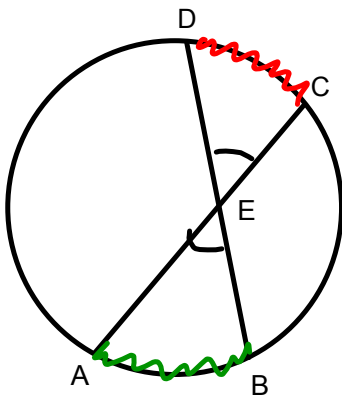


Tangent-chord Angle

$$m \angle GHI = \frac{1}{2} (m \text{ Arc } GH)$$

Example:

Given $m \text{ Arc } GH = 160^\circ$, Find $m \angle GHI$



Chord-chord Angle

$$m \angle DEC = \frac{1}{2} (m \text{ Arc } AB + m \text{ Arc } CD)$$

$$m \angle AEB = \frac{1}{2} (m \text{ Arc } AB + m \text{ Arc } CD)$$

$$m \angle DEA = \frac{1}{2} (m \text{ Arc } DA + m \text{ Arc } CB)$$

$$m \angle CEB = \frac{1}{2} (m \text{ Arc } DA + m \text{ Arc } CB)$$

Example 1:

Given $m \text{ Arc } BC = 112^\circ$

$m \text{ Arc } AD = 186^\circ$

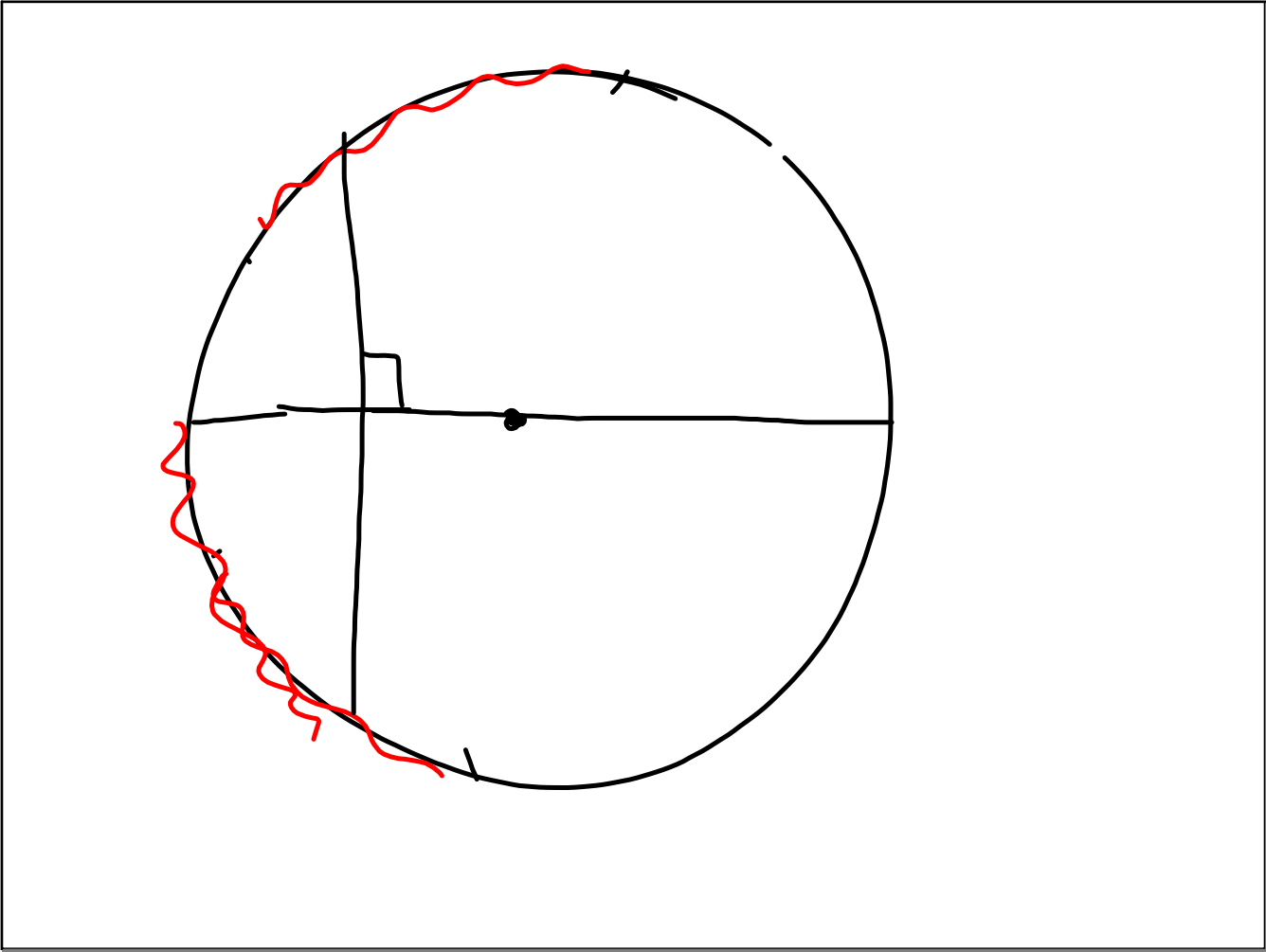
Find $m \angle DEA$

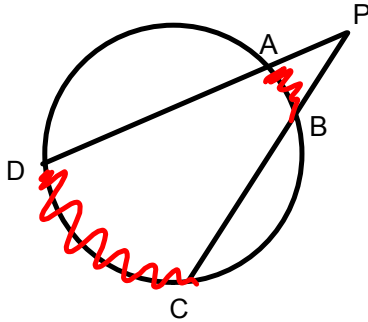
Example 2:

Given $m \angle DEC = 50^\circ$

$m \text{ Arc } AB = 72^\circ$

Find $m \text{ Arc } DC$





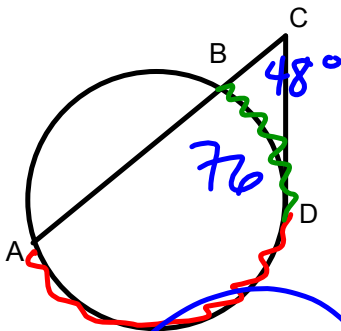
Secant-secant Angle

$$m \angle P = \frac{1}{2} (m \text{ Arc DC} - m \text{ Arc AB})$$

Example:

Given $m \text{ Arc DC} = 110^\circ$, $m \text{ Arc AB} = 32^\circ$

Find $m \angle P$



Secant-tangent Angle

$$m \angle C = \frac{1}{2} (m \text{ Arc AD} - m \text{ Arc BD})$$

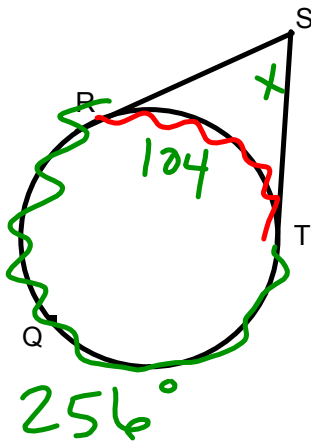
Example:

Given $m \text{ Arc BD} = 76^\circ$, $m \angle C = 48^\circ$

Find $m \text{ Arc AD}$

$$x = 172, \quad 48 = \frac{1}{2}(x - 76)$$

$$96 = x - 76$$



Tangent-tangent Angle

$$m \angle S = \frac{1}{2} (m \text{ Arc RQT} - m \text{ Arc RT})$$

Example:

Given $m \text{ Arc RT} = 104$, Find $m \angle S$

$$x = \frac{1}{2} (256 - 104) = 76$$

**Confused? See the summary on the next slide!
(and p. 472 of your textbook!)**

Summary

If the vertex is...

- **AT THE CENTER** the angle is **equal** to the intercepted arc
- **ON THE CIRCLE** the angle is **half** the intercepted arc
- **INSIDE THE CIRCLE** (not at center) the angle is **half the sum** of the intercepted arcs
- **OUTSIDE THE CIRCLE** the angle is **half the difference** of the intercepted arcs

Classwork

- 10.5 Angles Related to a Circle Worksheet

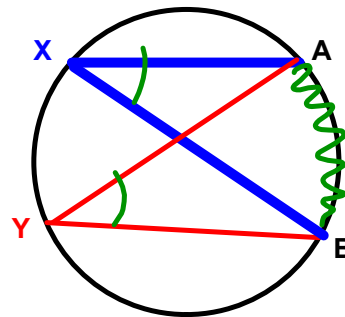


10.6 More Angle-Arc Theorems

Theorem: If two inscribed or tangent-chord angles intercept the same arc, then they are congruent.

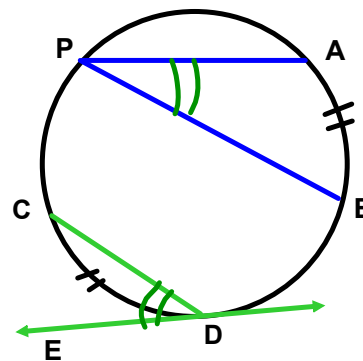
Given: X and Y are inscribed angles intercepting arc AB.

Conclusion: $\angle X \cong \angle Y$



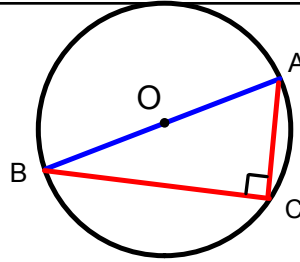
Theorem: If two inscribed or tangent-chord angles intercept congruent arcs, then they are congruent.

If \overleftrightarrow{ED} is the tangent at D and $\widehat{AB} \cong \widehat{CD}$
then we may conclude that $\angle P \cong \angle CDE$



Theorem: An angle inscribed in a semicircle is a right angle.

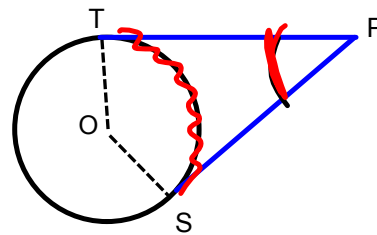
How can that be proven?



Theorem: The sum of the measures of a tangent-tangent angle and its minor arc is 180.

(not a secant-secant)
The $m\angle P + m\widehat{TS} = 180$

How can that be proven?



Read the Sample Problems

on pages 480 - 481

Homework

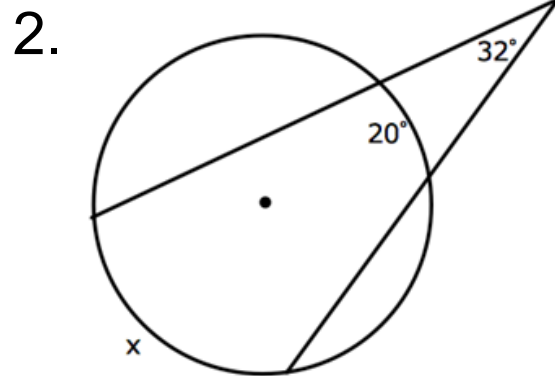
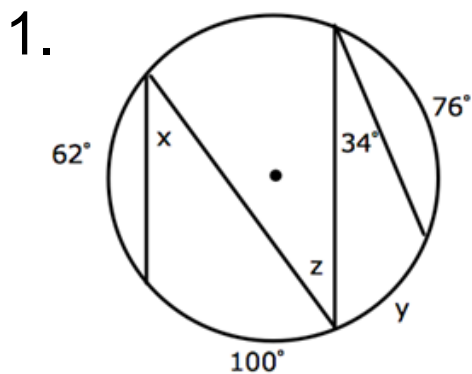
- 10.5 Angles Related to a Circle Worksheet
- p. 481 #~~5~~, 7, ~~10~~, 14



*If you didn't
finish in class*

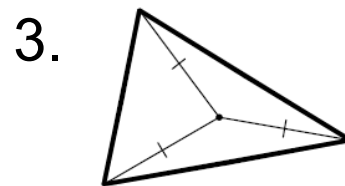
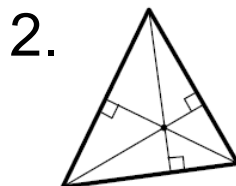
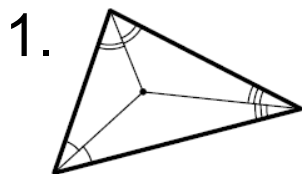
Exit Slip

Find the missing measures. SHOW WORK!



Name the point of concurrency shown.

(incenter, circumcenter, orthocenter or centroid)



EXIT SLIP

