

1. Find the ratio of the sides of the squares

(smaller to larger) $3:7$

2. Find the ratio of the perimeters of the squares

(smaller to larger) $3:7 \rightarrow 12:28$

3. Find the ratio of the areas of the squares

(smaller to larger) $9:49$

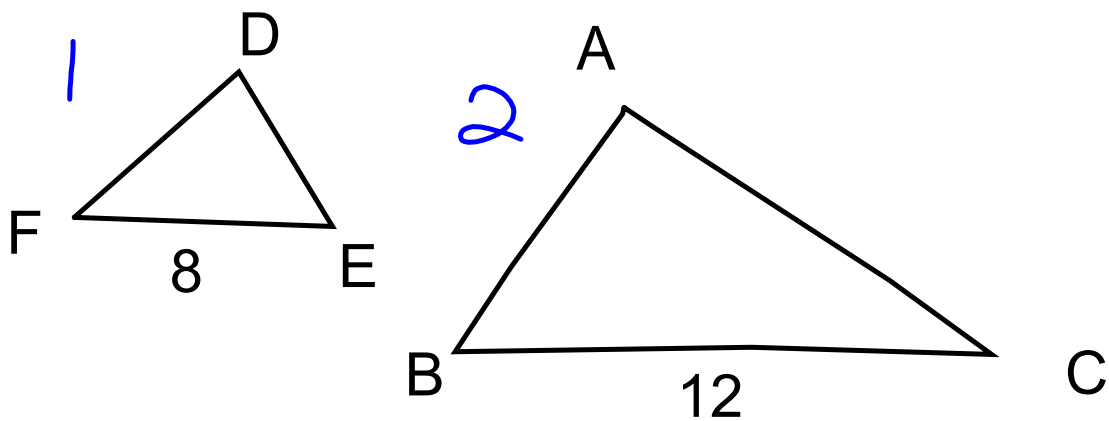
4. What do you notice?

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Similar-Figures Theorem: If two figures are similar, then the ratio of their areas equals the square of the ratio of corresponding segments.

$$\frac{A_1}{A_2} = \left(\frac{s_1}{s_2}\right)^2$$

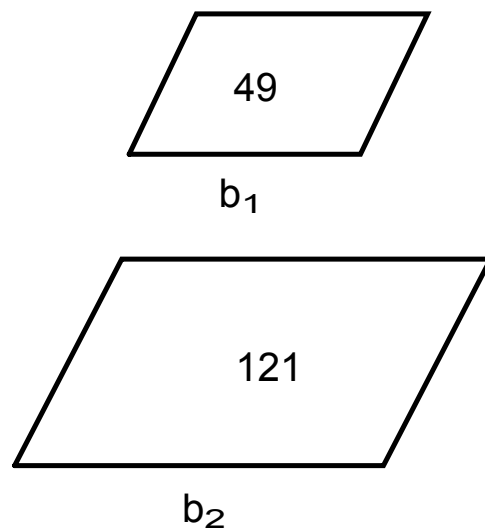
Where A_1 and A_2 are areas and s_1 and s_2 are measures of corresponding sides.



Triangles ABC and DEF are similar.
Find the ratio of their areas.

$$\frac{A_1}{A_2} = \left(\frac{8}{12}\right)^2 = \frac{64}{144} = \frac{4}{9}$$

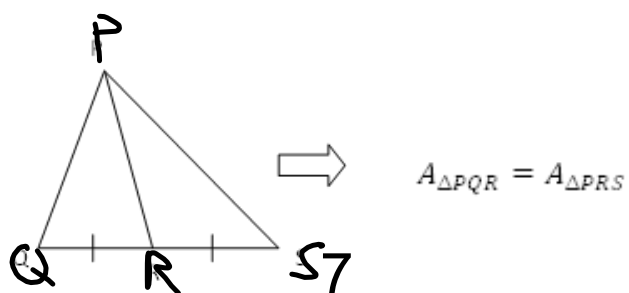
If the ratio of the areas of two similar parallelograms is 49:121, find the ratio of their bases.



$$\frac{7}{11} = \frac{\sqrt{49}}{\sqrt{121}} = \left(\frac{s_1}{s_2} \right)$$

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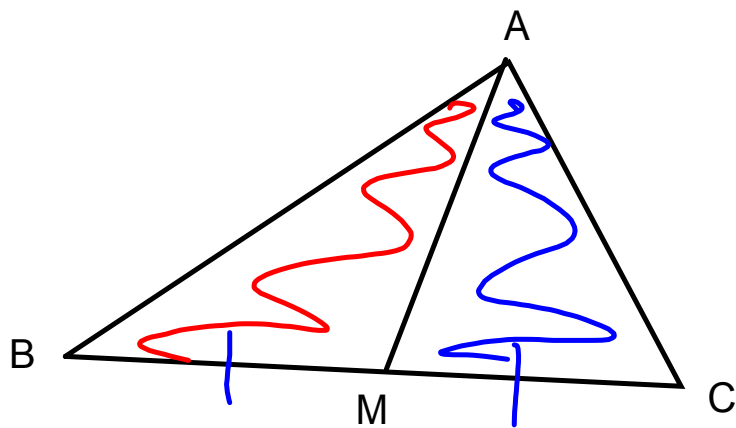
Theorem: A median of a triangle divides the triangle into two triangles with equal areas.



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AM is a
median of
triangle ABC.

Find the ratio
of the area of
triangle ABM
to the area of
triangle ACM



1:1

What formulas do you know to find the area of a triangle?

1) $\frac{1}{2}bh$

3) $\frac{1}{2}ab\sin C$

2) $\frac{1}{2}ap$

Which of the above formulas used?

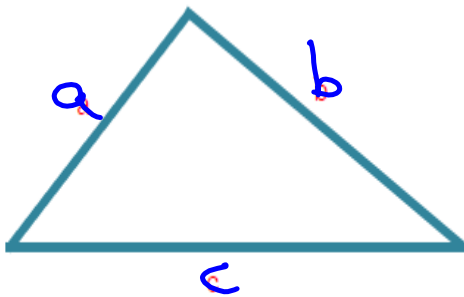
What if we have a different situation entirely?...

Theorem (Hero's Formula)

$$A_{\Delta} = \sqrt{s(s-a)(s-b)(s-c)},$$

where a , b , and c are the lengths of the sides of the triangle

$$\text{and } s = \text{semiperimeter} = \frac{a+b+c}{2}$$



$$A = \sqrt{s(s-a)(s-b)(s-c)}$$

Can be used to find the area of a triangle
when given SSS!

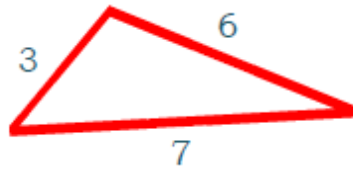
find the area of a triangle with sides 3, 6, and 7.

$$\sqrt{8(5)(2)(1)}$$

$$\sqrt{80}$$

$$4\sqrt{5}$$

$$\sqrt{16} \quad \sqrt{5}$$



Step 1: Find the perimeter $\rightarrow 16$

Step 2: Find the semiperimeter $\rightarrow 8$

Step 3: Replace variables in Hero's formula using corresponding values and evaluate!

Area of Cyclic Quadrilaterals

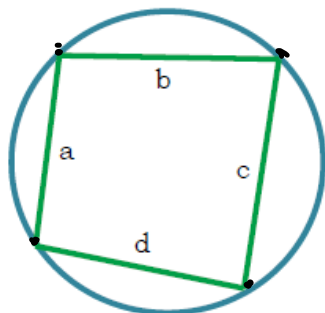
A Hindu mathematician named **Brahmagupta** recorded a formula for deriving the area of an **inscribed quadrilateral** in about 628 A.D. Brahmagupta's formula can only be applied to quadrilaterals that are **cyclic quadrilaterals**, meaning quadrilaterals that can be inscribed in circles.

Theorem (Brahmagupta's formula)

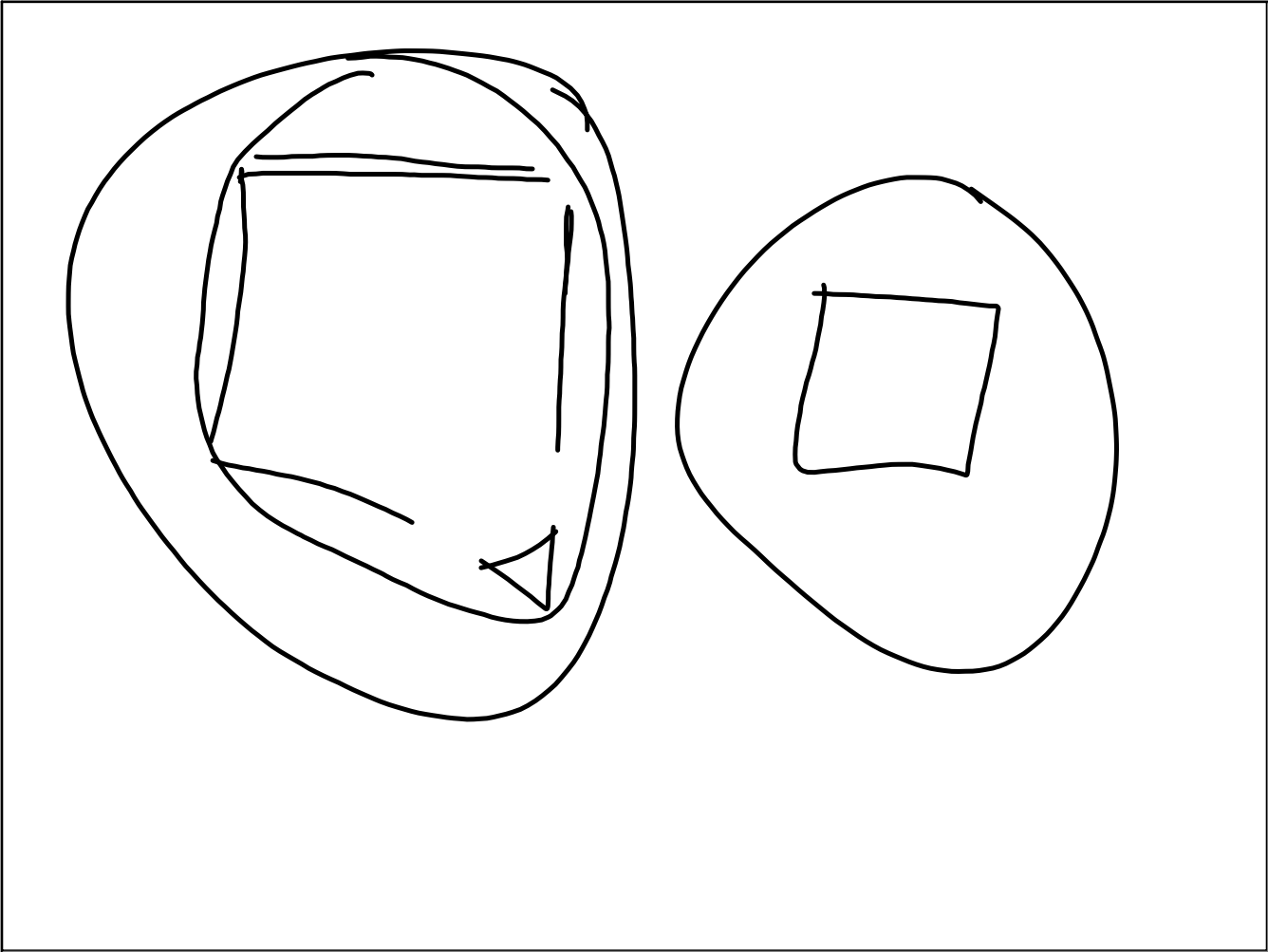
$$A_{\text{cyclic quad}} = \sqrt{(s-a)(s-b)(s-c)(s-d)},$$

where a , b , c , and d are the sides of the quadrilateral

and s = semiperimeter = $\frac{a+b+c+d}{2}$



☆ inscribed Quadrilaterals ☆



find the area of a cyclic quadrilateral

$$\sqrt{10 \cdot 5 \cdot 6 \cdot 3}$$

$$\sqrt{900}$$

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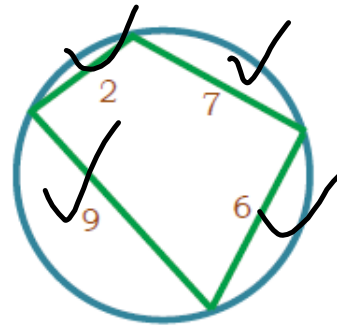
Step 1: Find the perimeter \rightarrow

24

Step 2: Find the semiperimeter \rightarrow

12

Step 3: Substitute corresponding values into Brahmagupta's formula and evaluate.



Classwork

Stations

Homework

43 p. 546 #4 - 8, 11 - 13, 15, 16

44 p. 551 #6, 9