## Warm Up

- Given: Angle MOR $=(3 x+7)^{\circ}$

Angle ROP $=(4 x-1)^{\circ}$
$\mathrm{MO} \perp \mathrm{OP}$

- Which angle is larger, angle MOR or angle ROP?

$$
3 x+7+4 x-1=90{ }^{m} \quad r^{R} \quad 3 x+7=4 x-1
$$

## Complementary and

## Supplementary Angles



## I CAN...

- Define and identify complementary and supplementary angles
- Write proofs involving complementary and supplementary angles


## Complementary Angles

- Two angles whose sum is $90^{\circ}$

- $\angle \mathrm{A}$ is complementary to $\angle \mathrm{B}$

- $\angle \mathrm{JOC}$ is the complement of $\angle \mathrm{COB}$


## Supplementary Angles

- Two angles whose sum is $180^{\circ}$

- $\angle \mathrm{A}$ is supplementary to $\angle \mathrm{B}$

- $\angle \mathrm{HAM}$ is the supplement of $\angle \mathrm{HAB}$


## Definitions: If-then Form

$$
\text { ad\& to } 90^{\circ}
$$

- If two angles form a right angle, then they are complementary.

$$
\text { add to } 180^{\circ}
$$

- If two angles form a straight angle, then they are supplementary.

Example 1

- Given: $\angle$ TVK is a right $\angle$
- Prove: $\angle 1$ is comp. to $\angle 2$

(2) $\angle T v x+\angle X v k=90^{\circ}$
(2) Assumed from diagrarn
$\left(L_{1}\right)+(\angle 2)$
(3) $\angle 1$ comp. ta $\angle 2$
(3) If 2 c's form a ort $c$, then they are comp.

Example 2

- Given: Diagram as shown
- Prove: $\angle 1$ is supp. to $\angle 2$


Example 3

- The measure of one of two complementary angles is three greater than twice the measure of the other. Find the measure of exch.


$$
\begin{aligned}
x+2 x+3 & =90 \\
x+2 x & =87 \\
3 x & =87 \\
x & =29
\end{aligned}
$$

Example 4

$$
180-x=
$$

- The measure of the supplement of an angle is 60 less than 3 times the measure of the complement of the angle. Find the measure of the complement.

$$
\begin{aligned}
\text { supp } & =180-x \\
\text { comp } & =90-x \\
180-x & =3(90-x)-60 \\
180-x & =270-3 x-60 \\
180-x & =210-3 x \\
2 x & =30 \\
x & =15
\end{aligned}
$$

## Groups of 2

- Work with your partner to complete the proof I give you.
- Write a paragraph proof.
- Be prepared to present your proof to the class!!
- Given: $\angle 1$ is supp. to $\angle 2$
$\angle 3$ is supp. to $\angle 2$
- Prove: $\angle 1 \cong \angle 3$

1


Write a paragraph proof:

- Given: $\angle 1$ is comp. to $\angle 2$


## $\angle 3$ is comp. to $\angle 2$

- Prove: $\angle 1 \cong \angle 3$


Write a paragraph proof:

- Given: $\angle \mathrm{A}$ is supp. to $\angle \mathrm{B}$

$$
\begin{aligned}
& \angle \mathrm{C} \text { is supp. to } \angle \mathrm{D} \\
& \angle \mathrm{~B} \cong \angle \mathrm{D}
\end{aligned}
$$

- Prove: $\angle \mathrm{A} \cong \angle \mathrm{C}$

Write a paragraph proof:

- Given: $\angle \mathrm{A}$ is comp. to $\angle \mathrm{B}$


## $\angle \mathrm{C}$ is comp. to $\angle \mathrm{D}$

 $\angle \mathrm{B} \cong \angle \mathrm{D}$- Prove: $\angle \mathrm{A} \cong \angle \mathrm{C}$

Write a paragraph proof:

## Theorem

comp.

- If two angles are supplementary to the same angle, then they are congruent.
- If $\angle 1$ is supp. to $\angle 2$ and
$\angle 3$ is supp. to $\angle 2$,
then $\angle 1 \cong \angle 3$.

$$
\begin{aligned}
& \text { H Alsowark } \\
& \text { w/ comp }
\end{aligned}
$$

## Theorem

- If two angles are supplementary to congruent angles, then they are congruent.
- If $\angle A$ is supp. to $\angle B$,
$\angle C$ is supp. to $\angle D$, and $\angle B \cong \angle D$.
then $\angle A \cong \angle C$.



## Theorem

- If two angles are complementary to the same angle, then they are congruent.
- If $\angle 1$ is comp. to $\angle 2$ and $\angle 3$ is comp. to $\angle 2$,
then $\angle 1 \cong \angle 3$.



## Theorem

- If two angles are complementary to congruent angles, then they are congruent.
- If $\angle A$ is comp. to $\angle B$, $\angle C$ is comp. to $\angle D$, and $\angle B \cong \angle D$,
then $\angle A \cong \angle C$.



## Homework

- p. 69 \# 7,8,10,11, 16, 21
- Read Sample Problems on pages 77 \& 78
- p. 79 \# 1, 3, 5,8, 14

